

These are only a *few* sample problems to help you prepare for the exam.

You should also be certain that you completely understand the WebWork assignments, Problems Sets, in-class work, and your class notes.

1. Do the following series diverge, converge conditionally, or converge absolutely?

$$(a) \sum_{n=1}^{\infty} (-1)^n \frac{n}{\pi n - 1} \quad (b) \sum_{r=10}^{\infty} \frac{(-1)^r}{r + 6} \quad (c) \sum_{k=1}^{\infty} (-1)^k \frac{2k}{k^3 + 2}$$

2. Is it possible that the terms of a series converge but the partial sums diverge?
Can the partial sums converge but the terms diverge? Explain.

3. Evaluate $\sum_{k=2}^{326} \left(\frac{3}{7}\right)^k$ by hand.

4. Find the interval of convergence for the power series

$$(a) \sum_{k=0}^{\infty} 3^k x^k \quad (b) \sum_{k=1}^{\infty} \frac{(x-4)^k}{k2^k}$$

5. Let $f(x)$ be a continuous function that is positive and decreasing for all $x \geq 1$. Let $a_k = f(k)$. Rank the following values. Draw diagrams to explain your answer.

$$A = \sum_{k=5}^{n-1} a_k \quad B = \sum_{k=6}^n a_k \quad C = a_5 + \int_6^n f(x) dx \quad D = \int_5^n f(x) dx$$

6. Show that the following series converge. How accurately does S_{75} approximate the exact value of the series?

$$(a) \sum_{k=6}^{\infty} (-1)^k \frac{17}{k! + k^2} \quad (b) \sum_{k=3}^{\infty} \frac{\sin(k)}{k^5 + \ln(k)} \quad (c) \sum_{k=1}^{\infty} 2k^2 e^{-k^2}$$

7. Calculate $\int_0^1 \cos(x^2) dx$ accurate within 0.001 *by hand without the use of a calculator*.

8. Give examples that demonstrate why the Ratio Test is inconclusive when $\lim_{k \rightarrow \infty} \frac{a_{k+1}}{a_k} = 1$.

That is, give an example of a convergent series with this property and another example of a divergent series with this property.

9. Approximate $\sqrt[3]{e}$ accurate within 0.001 by hand. *Hint: $\sqrt[3]{e} = e^{\frac{1}{3}}$*